

Príklad: Zjednodušte výrazy

$$a) \frac{a^3+b^3}{a^2+b^2+2ab} = \frac{a^2-ab+b^2}{a+b} \quad [a \neq -b]$$

$$b) \frac{x^4-2x^3y+y^2x^2}{x^4-x^3y} = \frac{x-y}{x} \quad [x \neq 0, x \neq y]$$

$$c) \frac{1}{a+1} - \frac{2a}{a^2-1} = \frac{1}{1-a} \quad [a \neq \pm 1]$$

$$d) \frac{a^4-2a^3b+a^2b^2}{2a^3(a-b)} = \frac{a-b}{2a} \quad [a \neq 0, a \neq b]$$

$$e) (2\sqrt{3} + \sqrt{5})^2 - 2\sqrt{60} = 17$$

$$f) \frac{\sqrt{2}-\sqrt{3}}{1-\sqrt{2}} = -2-\sqrt{2}+\sqrt{3}+\sqrt{6} = (\sqrt{3}-\sqrt{2}) \cdot (1+\sqrt{2})$$

$$g) \sqrt{x^{\frac{1}{3}} \cdot x} : \sqrt[3]{(\sqrt{x} \cdot x^{-2})^2} = x^{\frac{5}{3}} \quad [x > 0]$$

$$h) (10^{\frac{1}{3}} 8^{-\frac{1}{2}})^{-3} (5^{\frac{1}{4}} 4^{\frac{1}{8}})^{-2} = 2^3 \cdot 5^{-\frac{3}{2}}$$

$$i) \sqrt{a \cdot \sqrt[3]{b}} : \sqrt[3]{b^{-1} \sqrt{a^3}} = b^{\frac{1}{2}} \quad [a > 0, b > 0]$$

$$j) \sqrt[5]{\frac{4}{\sqrt[3]{2}}} : \sqrt[3]{\frac{2}{\sqrt[5]{8}}} = 2^{\frac{1}{5}} = \sqrt[5]{2}$$

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$$(k) \left(\frac{1+\sqrt{3}}{1+|2-\sqrt{3}|} + \frac{2}{1-\sqrt{3}} \right) = 1 \quad \leftarrow \text{NESTÍHLI JSME ZADAT ANI SPOČÍTAT}$$

$$\begin{aligned} (a \pm b)^2 &= a^2 \pm 2ab + b^2 \\ (a \pm b)^3 &= a^3 \pm 3a^2b + 3ab^2 \pm b^3 \\ a^2 + b^2 &= a^2 + b^2 \\ a^2 - b^2 &= (a+b)(a-b) \\ a^3 + b^3 &= (a+b)(a^2 - ab + b^2) \\ a^3 - b^3 &= (a-b)(a^2 + ab + b^2) \end{aligned}$$

$$\begin{aligned} x^a \cdot x^b &= x^{a+b} \\ \frac{x^a}{x^b} &= x^{a-b}; x^b = x^{a-b} \\ \frac{1}{x^b} &= x^{-b} \\ (x^a)^b &= x^{ab} \\ (xy)^a &= x^a y^a \\ \sqrt[n]{x} &= x^{\frac{1}{n}} \\ \sqrt[n]{x^a} &= x^{\frac{a}{n}} \end{aligned}$$